



Technion - Israel Institute of Technology  
Department of Electrical Engineering  
**Signal and Image Processing Laboratory**



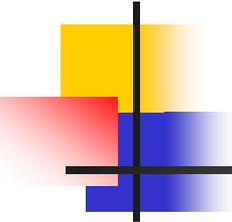
# Packet Loss Concealment for Audio Streaming based on GAPES and MAPES Algorithms

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IEEE Conference – Eilat, Israel





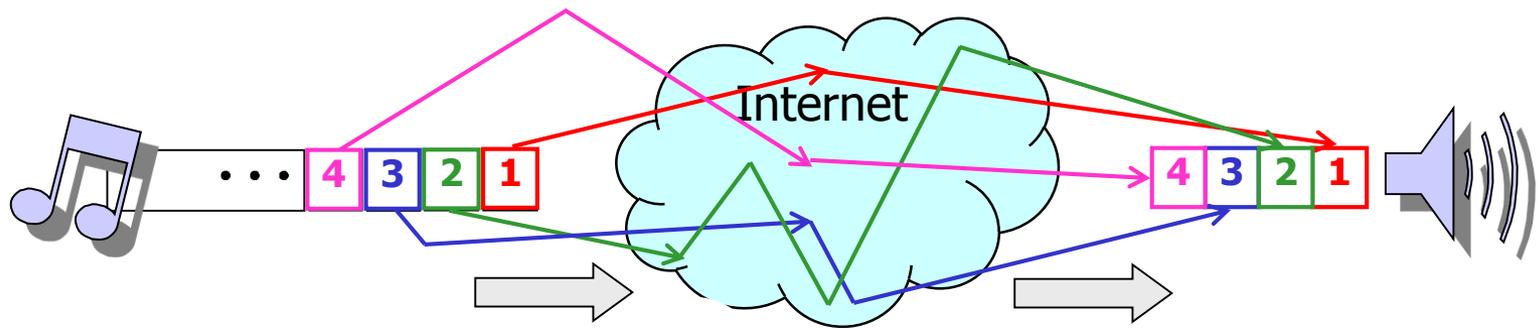
# Presentation Outline

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- Introduction to Packet Loss
- Previous Works
- MPEG-audio compression
- Proposed concealment algorithm
  - Concealment domain
  - GAPES and MAPES interpolation algorithms
- Subjective tests results
- Conclusion

# Internet Audio Streaming

- A Real-Time application.
- Connectionless protocol:  
Each packet may use a different route.



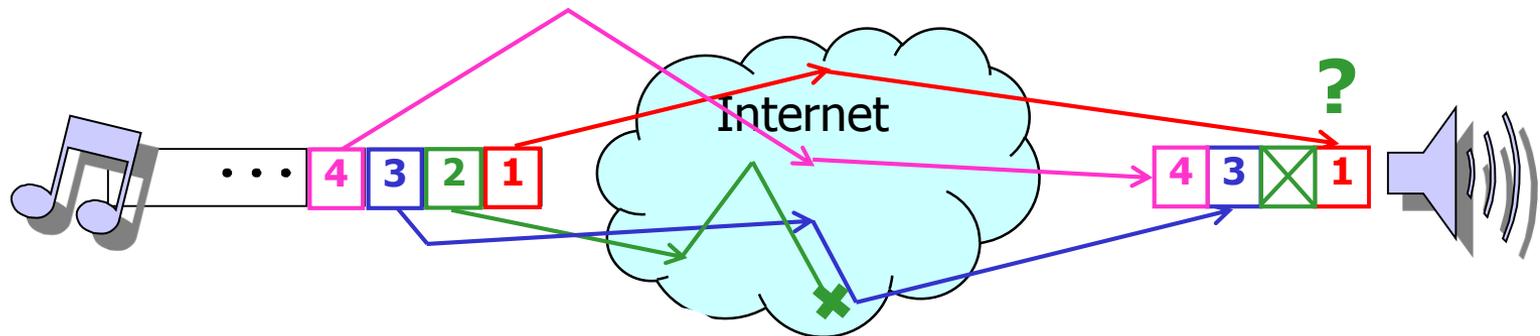
Audio signal frames  
are compressed into  
data packets

The packets are  
consecutively sent  
over the internet

The receiving packets  
are reassembled,  
decompressed and  
played

# Packet Loss

- Internet broadcasting doesn't assure quality of service (QoS).
  - Data packets are often delayed or discarded during network congestions.



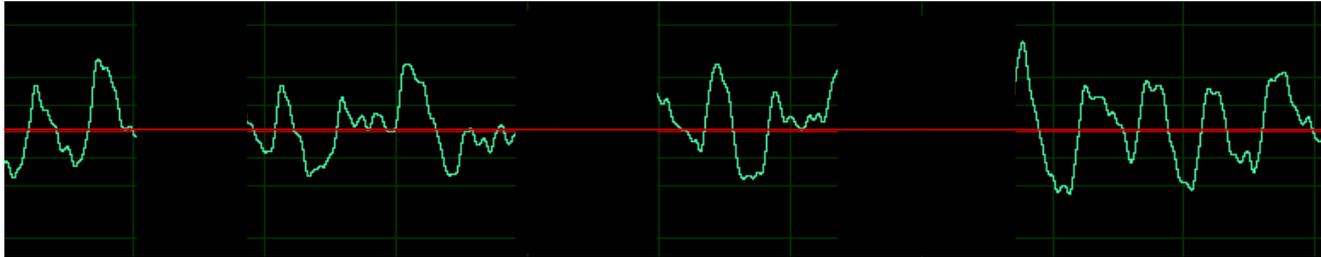
- Each loss, unless concealed, produces an annoying disturbance.

■ Example:

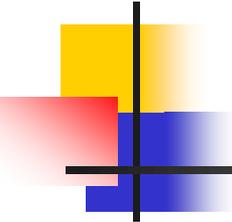
Original	10% loss	30% loss
		30% Repaired

# Packet Loss Concealment

- Fill-in the gap with an approximation to the original signal.



- Goal: Generate a good enough replacement.
  - Good enough = won't be noticed by a human listener.
- Problem
  - A typical audio packet takes around 1000 samples.
  - Even a single lost packet creates a very wide gap that is difficult to interpolate.
- So, what is the best concealment method?...



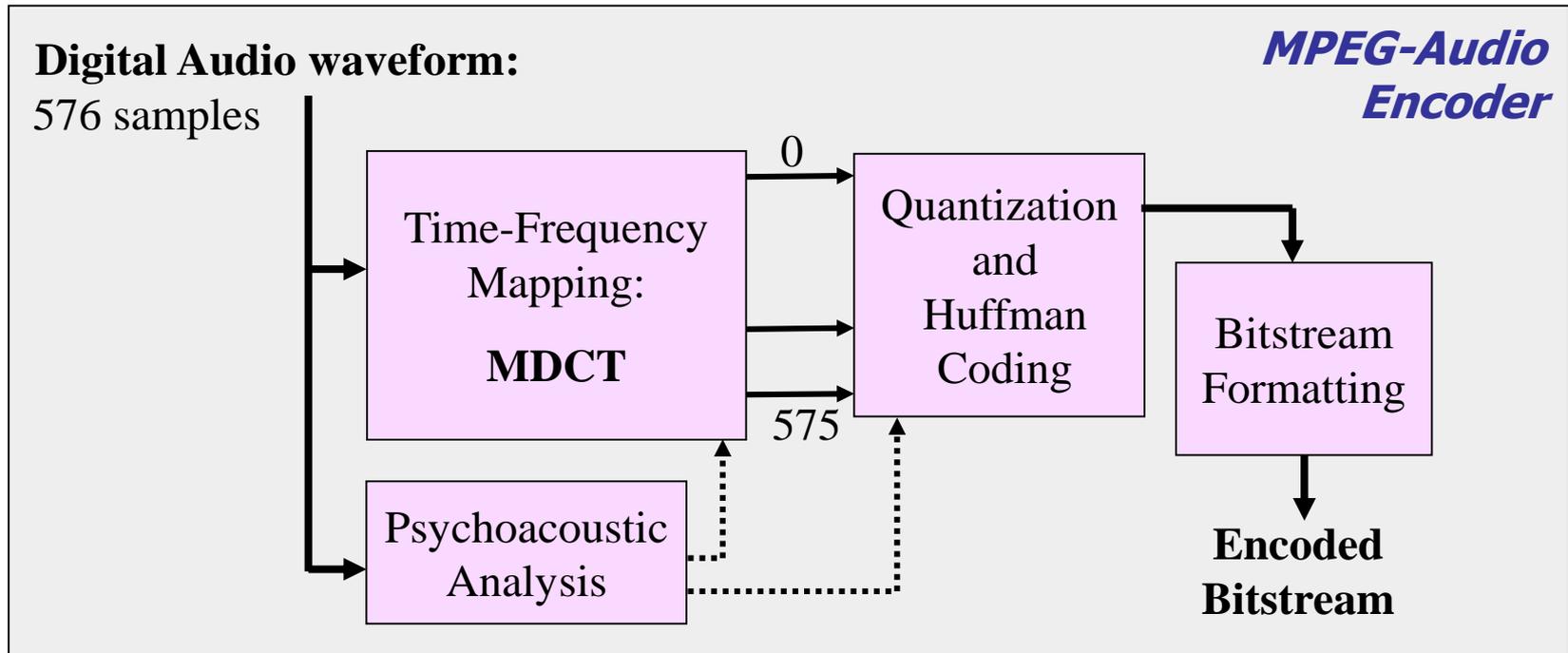
# Previous works

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- Receiver-based techniques:
  - Waveform substitution (off-line)
  - Packet repetition
  - Statistical Interpolation
  - GAPES in the DSTFT domain

# MPEG-Audio Coder

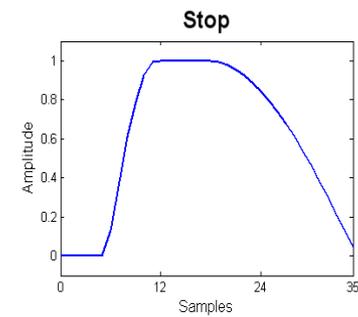
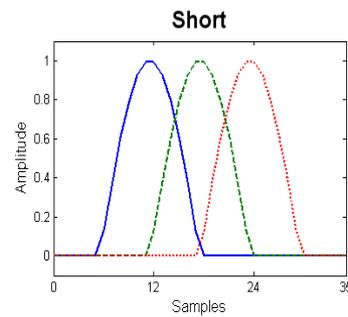
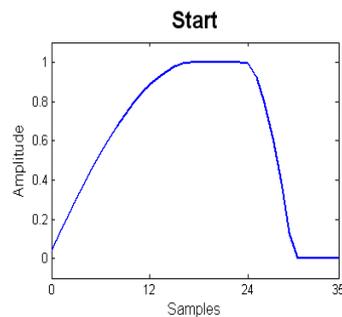
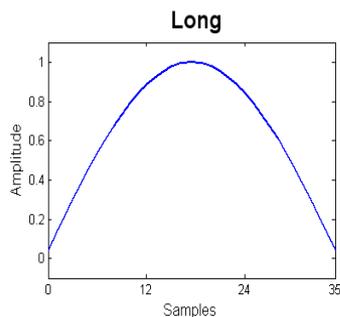
- Perceptual audio coders.
- MP3: Every two frames form an **MP3 packet**.

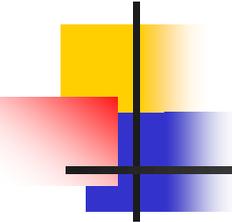


One lost MP3 packet (1152 samples) is equivalent to **only** 2 lost MDCT coefficients per frequency bin!

# MDCT

- $2N$  time samples  $\rightarrow N$  MDCT real-valued coefficients
- **Lossless** transform if windows overlap
- Reconstruction using overlap & add
- MP3 defines 4 window functions for the MDCT.
  - **Long**: better frequency resolution for stationary segments.
  - **Short**: better time resolution for transients.





# Concealment in MDCT domain

Q consecutive missing packets are equal to...

- Time domain:  $(2Q+1) \cdot 576$  missing samples.
- ☑ MDCT domain:  $2Q$  missing coeff. per frequency bin.

However...

- MDCT coefficients along time show rapid sign changes.

Solution: Use a domain with less signal fluctuations.

- Different windows → different frequency resolutions.

Solution: Use a single window type when converting the data to another domain.

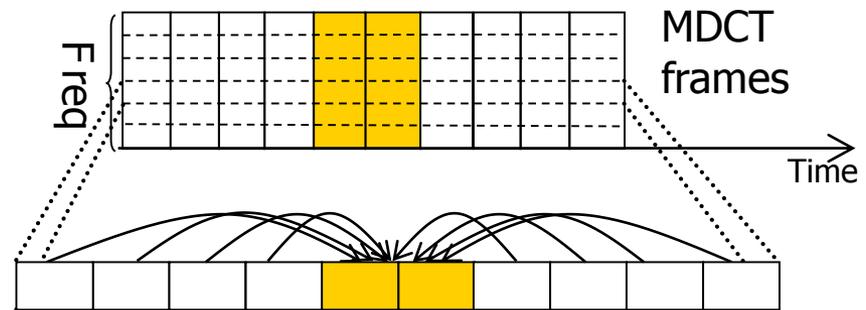
**Our choice:** The DSTFT domain

# Example: Solution in MDCT domain

- Statistical Interpolation (SI)

[Quackenbush and Driessen, 115th AES conv., Oct. 2003]

- Each frequency bin along time is reconstructed separately.



- Benefits: Applied directly in the compressed domain.
- Limitations: Limited loss patterns, high complexity, assumes parametric model.

# MDCT $\leftrightarrow$ DSTFT Conversion

## ■ Issues:

- FFT cannot be used in conversion.
- 4 MDCT windows  $\rightarrow$  12 different conversion expressions.



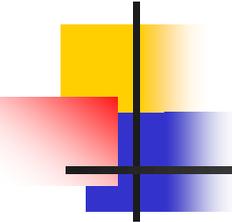
## Solution

A single expression for each conversion direction.

## ■ For example, MDCT $\rightarrow$ DSTFT Conversion:

$$X_n^{DSTFT}[m] = \sum_{k=0}^{N-1} X_n^{MDCT}[k] \cdot \left( g_d^1[m, k] + (-1)^m \cdot g_r^2[m, k] \right) \quad , 0 \leq m \leq N$$
$$+ \sum_{k=0}^{N-1} X_{n-1}^{MDCT}[k] \cdot g_d^2[m, k] + \sum_{k=0}^{N-1} X_{n+1}^{MDCT}[k] \cdot \left( (-1)^m \cdot g_r^1[m, k] \right)$$

- $g_{d/r}^1[m, k], g_{d/r}^2[m, k]$  (calculated off-line) are selected according to window types of frames  $X_{n-1}, X_n, X_{n+1}$ .
- Efficient conversion: operations number reduced by factor 3.



# APES-based Interpolation Algorithms

- APES: Amplitude and Phase Estimation (Stoica & Li, 1999).
  - An algorithm for spectral estimation.
- GAPES: Gapped-data APES (Stoica & Larsson, 2000).
  - Uses an adaptive filter-bank approach.
- MAPES: Missing-data APES (Stoica & Wang, 2005).
  - Uses an ML- estimator approach.
  - MAPES has lower complexity and can handle more loss patterns.

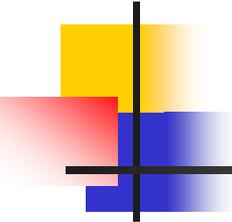
## Comparison to SI

### Benefits

- Can handle many loss patterns.
- Doesn't assume parametric modeling.
- Can be applied on complex signals.

### Limitations

- Higher complexity



# The APES Algorithm

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- Let  $\{x_n\}$  be a data-sequence of length P.

## Problem

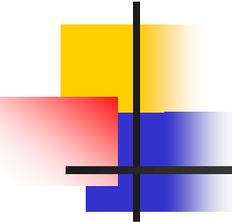
Estimate spectral component at frequency  $\omega_0$ :  $\alpha(\omega_0)$ .

## Solution

- $x_n$  is modeled as:  $x_n = \alpha(\omega_0) \cdot e^{j\omega_0 n} + e_n(\omega \neq \omega_0)$
- Design a narrow-band filter  $\underline{h}(\omega_0)$ , of length M:
  - The filter should pass the frequency  $\omega_0$  without distortion.
  - The filter should attenuate all the other frequencies.
- By filtering  $\{x_n\}$  with the filter  $\underline{h}(\omega_0)$  we get:

$$\underline{h}(\omega_0) * x_n \approx \alpha(\omega_0) \cdot e^{j\omega_0 n}$$

- Use DFT on the filtered data to estimate  $\alpha(\omega_0)$ .



# The APES Algorithm – Cont.

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- Description as a minimization problem:

$$\min_{\omega} \left\| \underline{h}(\omega) \cdot \underline{a}(\omega) \right\|$$

Where:

$\underline{h}(\omega) \in \mathbb{C}^{M \times 1}$  is a data-dependent narrow-band filter, centered at  $\omega_0$ .

$\underline{a}(\omega) \triangleq [1, e^{j\omega}, \dots, e^{j\omega(M-1)}]^T \in \mathbb{C}^{M \times 1}$  is a vector of exponents.

# The GAPES Algorithm

- APES is expanded to a frequency grid:  $\{\omega_k\}$ ,  $0 \leq k \leq K$ .
- The **missing samples**,  $\{x_m\}$ , are restored by solving the following minimization problem:

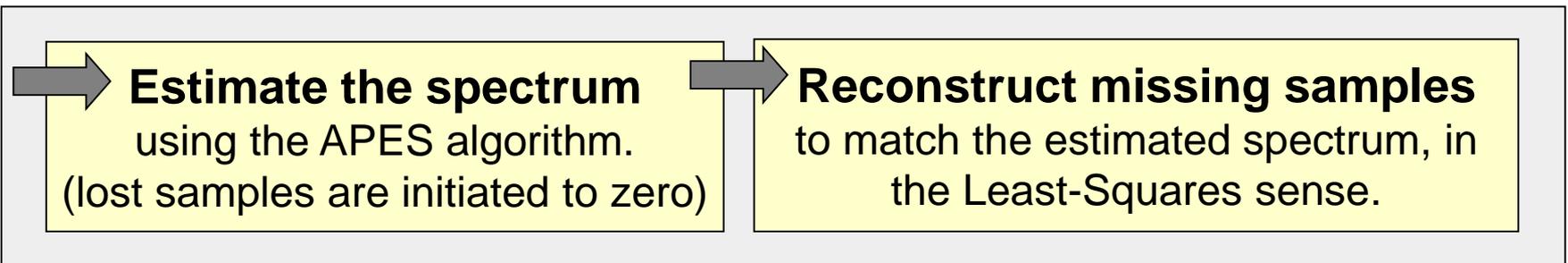
$$\min_{\{x_m\}, \{\alpha_k, \underline{h}_k\}} \sum_{k=0}^{K-1} \sum_{l=0}^{P-M} \left| \underline{h}_k^H \cdot \underline{x}_l - \alpha_k \cdot e^{j\omega_k l} \right|^2, \text{ subject to } \underline{h}_k^H \cdot \underline{a}_k = 1$$

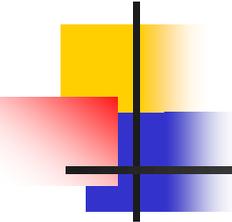
$\alpha_k \triangleq \underline{\alpha}(\omega_k)$  is the spectral component at frequency  $\omega_k$ .

$\underline{h}_k \triangleq \underline{h}(\omega_k)$  is a data-dependent narrow-band filter, centered at  $\omega_k$ .

$\underline{a}_k \triangleq \underline{a}(\omega_k)$

- Iterative algorithm. A single iteration:





# The APES Algorithm – Different Approach

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- APES has also an **ML- estimator** interpretation.
- Assuming  $\{\underline{e}_l(\omega_0)\}$  are statistically-independent, zero-mean complex Gaussian random vectors, with unknown covariance matrix:  $\mathbf{Q}(\omega_0)$ .
  - APES only approximates an ML- estimator since the vectors contain overlapping data !
- Under these assumptions, the ML- estimator:

# The MAPES Algorithm

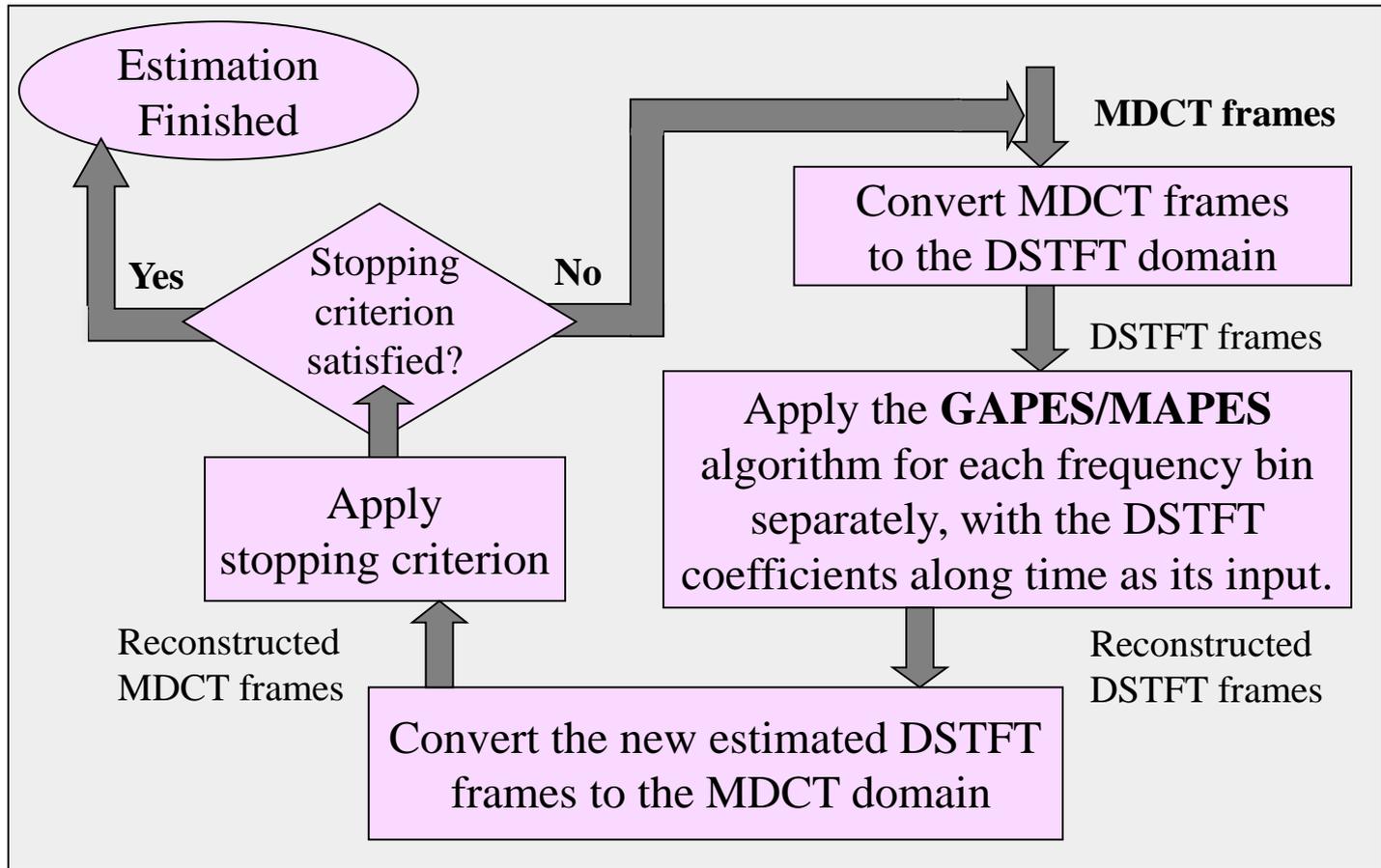
- The **missing samples**,  $\{x_m\}$ , are restored by solving the following maximization problem:

$$\max_{\{x_m\}, \{\alpha_k, \mathbf{Q}_k\}_{k=0}^{K-1}} \sum_{k=0}^{K-1} \log \left( Pr \left\{ \{\underline{x}_l\}_{l=0}^{P-M} \mid \alpha_k, \mathbf{Q}_k \right\} \right)$$

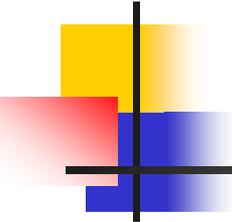
Where  $\mathbf{Q}_k$  is the covariance-matrix of the  $\{\underline{e}_l(\omega_k)\}$  vectors.

- Solved using an iterative algorithm that contains two steps:
  - Solve with respect to  $\{\alpha_k, \mathbf{Q}_k\}$  by applying APES.
  - Solve with respect to the missing samples.
- Lower complexity due to simple calculation process.

# Proposed Concealment Algorithm



*A block diagram of the reconstruction process*



# Results

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- Perceptual quality evaluation
  - Proposed solution (GAPES/MAPES) sounds better than previous works.
  - GAPES has small advantage over MAPES.
- Complexity
  - Proposed solution (GAPES/MAPES) is more complex than previous works.
  - MAPES has lower complexity than GAPES.

## Example:

- For 4 missing frames in a buffer of 16, GAPES requires twice the number of multiplications needed by MAPES.

# Audio Examples

## Example 1:

Piano Original

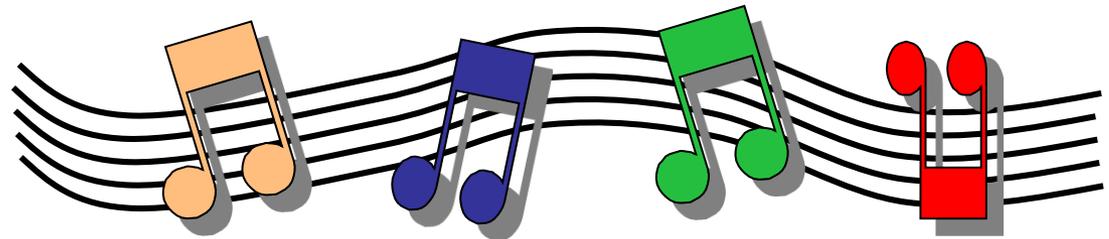
No concealment  
(30% random loss)

SI

Repetition

Proposed Algorithm  
(GAPES)

Proposed Algorithm  
(MAPES)



## Example 2:

Flute Original

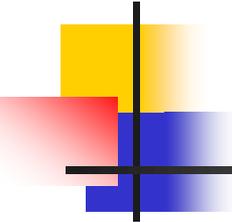
No concealment  
(20% random loss)

MAPES

GAPES

Repetition

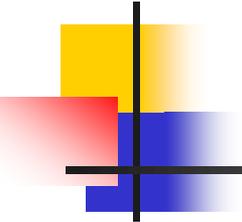
SI



# Conclusion

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- A new algorithm for packet loss concealment.
  - For audio streaming, encoded by MPEG-audio coders.
  - By applying GAPES or MAPES in the DSTFT domain.
- A direct conversion scheme was introduced:  
MDCT  $\rightleftharpoons$  DSTFT.
  - Enables efficient conversion between domains.
- Proposed algorithm performs better than packet repetition and statistical interpolation.
- MAPES is more robust than GAPES and needs lower complexity.



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# Thank You

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