



Technion - IIT  
Dept. of Electrical Engineering  
Signal and Image Processing Lab

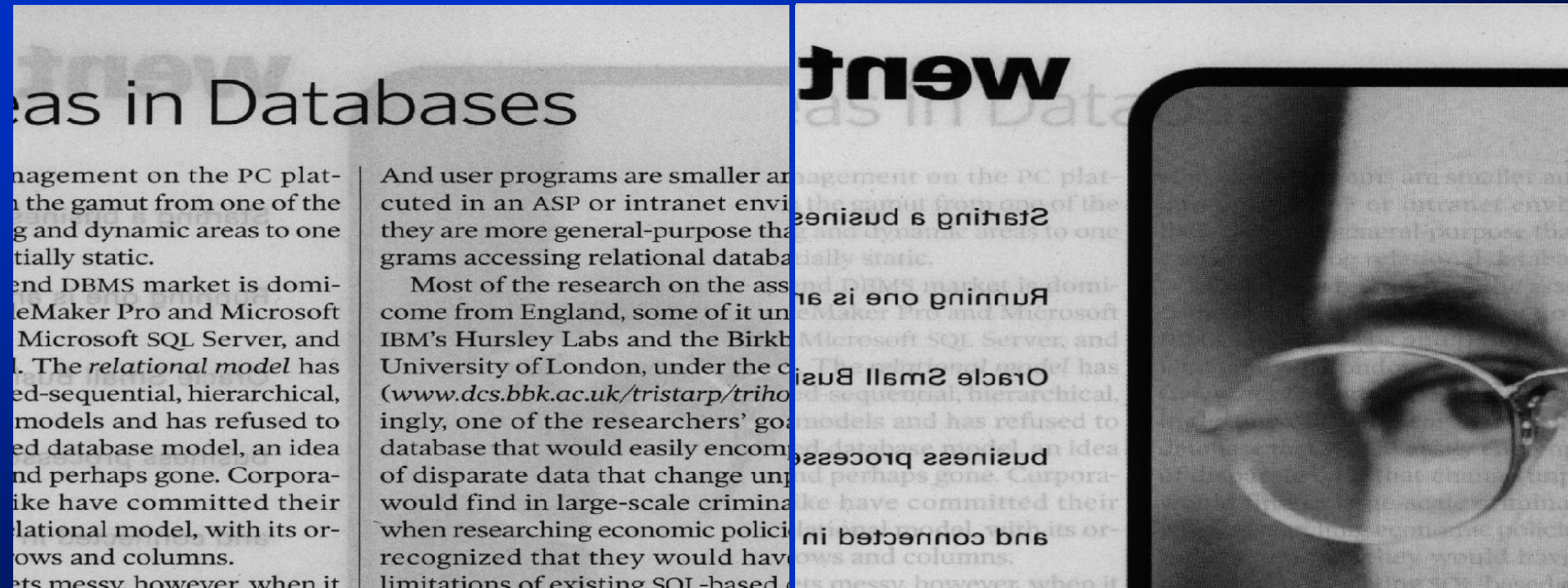


# *Show-Through Cancellation in Scanned Images*

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*M.Sc. Research under the supervision  
of Prof. David Malah*

# Show-Through in Scanned Images



Goal : Remove cross-talk from images without distortion.

# Talk Outline

- Previous work
- Physical model
- Decorrelation algorithm
  - Basic algorithm
  - Automatic background estimation
  - Local background normalization
  - Adaptive post-processing
  - Cascaded filter structure
- BSS algorithm
  - TV Regularization
  - Fidelity/Regularization Tradeoff
  - ICM
- Conclusions and Future work

# Previous Work

## Show-Through Removal in Scanned Images

- Sharma (<sup>01</sup>)

## Image Mixtures (Separating Reflections)

- Farid & Adelson (<sup>99</sup>) – linear mixtures, ICA
- Schechner, Kiryati & Basri (<sup>00</sup>) – convolutive mixtures, mutual information
- Bronstein<sup>2</sup>, Zibulevsky & Zeevi (<sup>03</sup>) – sparse ICA
- Sarel & Irani (<sup>04</sup>) – spatially varying linear mixtures
- Levin, Zomet & Weiss (<sup>04</sup>) – single image
- Tonazzini *et al* (<sup>01-05</sup>) – linear pointwise and convolutive image mixtures, MRFs

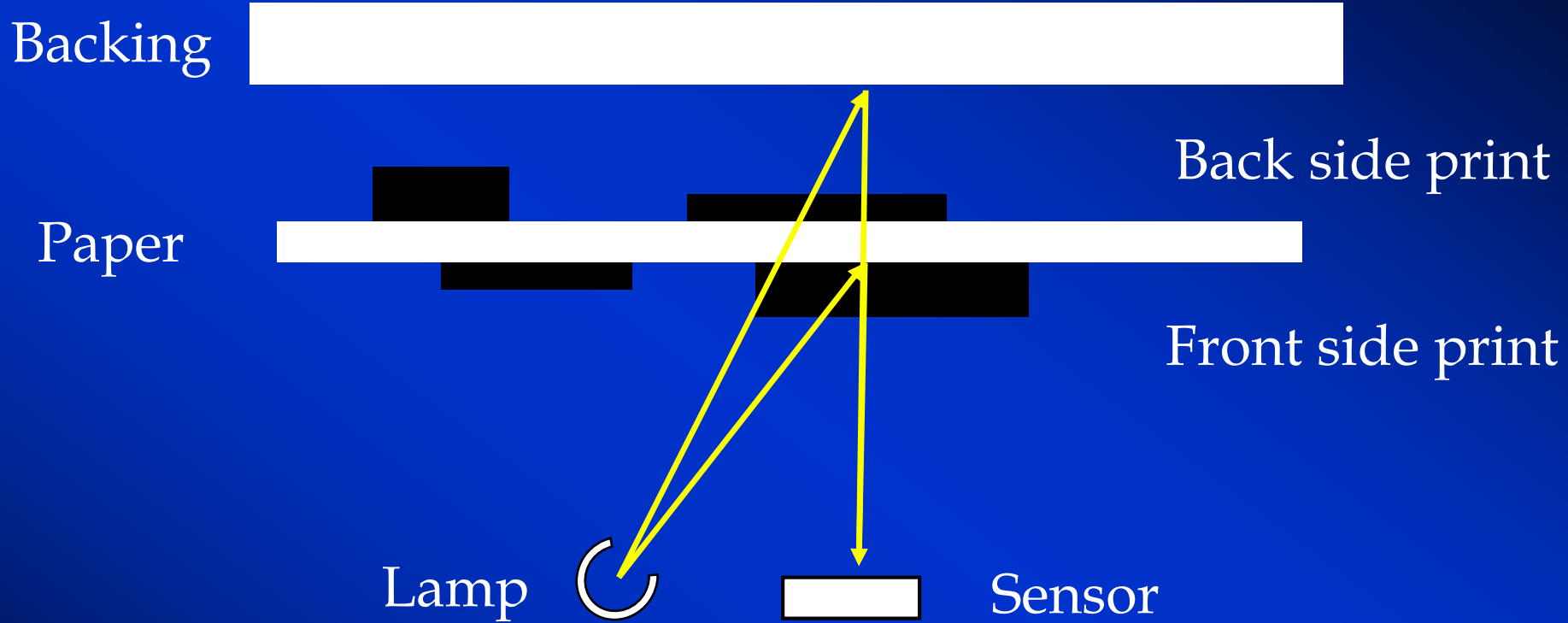
## Related Problems

- Multi-channel systems : Weinstein, Feder & Oppenheim (<sup>93</sup>), Thi & Jutten (<sup>95</sup>) – BSS of convolutive mixtures
- Deconvolution : Bronstein<sup>2</sup>, Zibulevsky & Zeevi (<sup>05</sup>) - sparsity, Chan & Wong (<sup>98</sup>) , Kaftory, Sochen & Zeevi (<sup>05</sup>)– TV, many others...

# Physical Model



# Physical Model - 1



$$R_f^s = R_{fp}^2 (R_p^2 + T_{fp}^2 R_{pbk} R_{bk}^2 T_b^2)$$

$$R_f = T_f^2 (R_p + T_p^2 R_{bk})$$

R - Reflectance  
T - Transmittance

# Physical Model - 2

## Definitions:

Reflectance of white paper:

$$R_p^w = R_p + T_p^2 R_{bk}$$

Normalized Optical  
Density

$$D = -\ln \frac{R}{R_p^w}$$

Normalized Optical  
Absorptance

$$A = 1 - \frac{R}{R_p^w}$$

## Linearized Creation Model:

$$D_f^s(x, y) \approx D_f(x, y) + \frac{T_p^2 R_{bk}}{R_p + T_p^2 R_{bk}} h(x, y) * AA(x, y)$$

# Show-Through Removal by Decorrelation



# Basic Cleaning Algorithm

(Sharma 2001)

- $R_p^w$  - Manual estimation.
- Front-side reflectance  $\rightarrow$  Density.
- Back-side reflectance  $\rightarrow$  Absorptance.
- For each pixel (progressing in a spatial contiguous order):
  - Compute show-through corrected density:

$$D_f(m, n) = D_f^s(m, n) - \sum_{k=-N}^N \sum_{l=-N}^N w(k, l) A_b^s(m-k, n-l)$$

- If back side has activity but not front side, update filter coefficients by LMS method:

$$w'(k, l) = w(k, l) + \mu D_f(m, n) A_b^s(m-k, n-l)$$

$$w(k, l) = w'(k, l)$$

- Convert density to reflectance.

# Results - Sharma

## as in Databases

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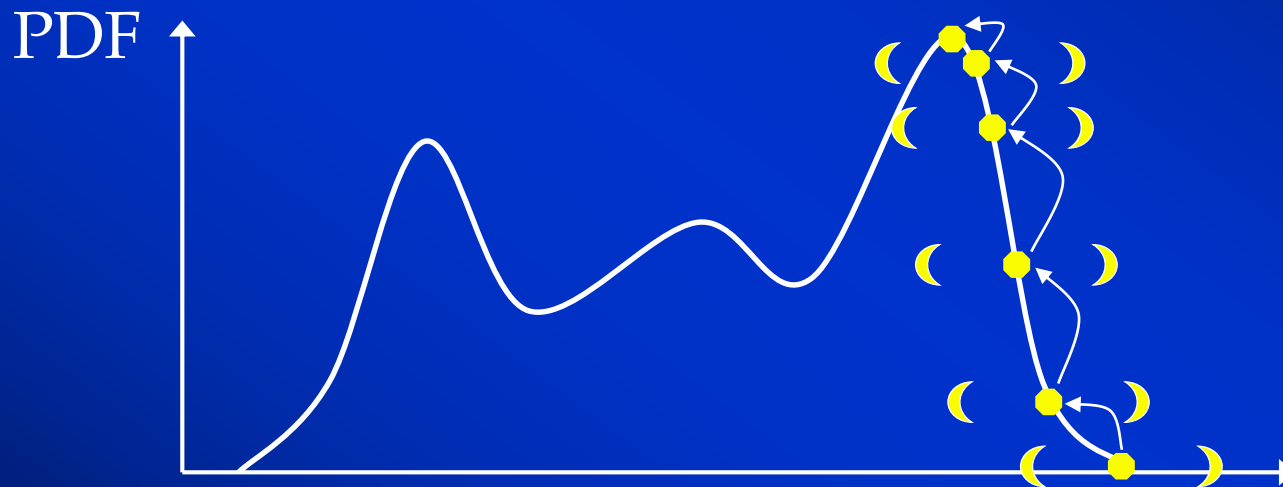
	Before	After
Corr	0.25	0.05
MI	0.1	0.02



# Automatic Background Estimation

Mean-Shift algorithm (Fukunaga ('75), Cheng ('95), Meer ('02)) :

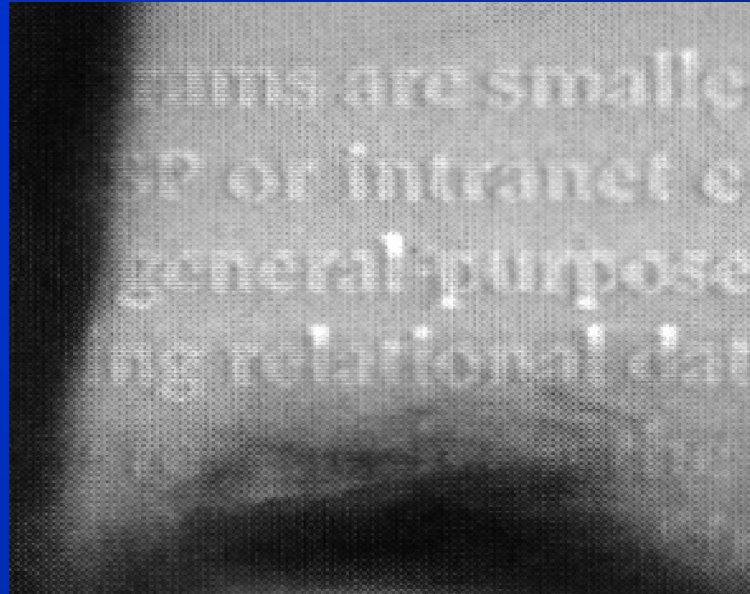
- Iterative steepest ascent algorithm
- Converges to local maximum



- Start point – brightest pixel
- Window size – proportional to signal STD

# Local Background - 1

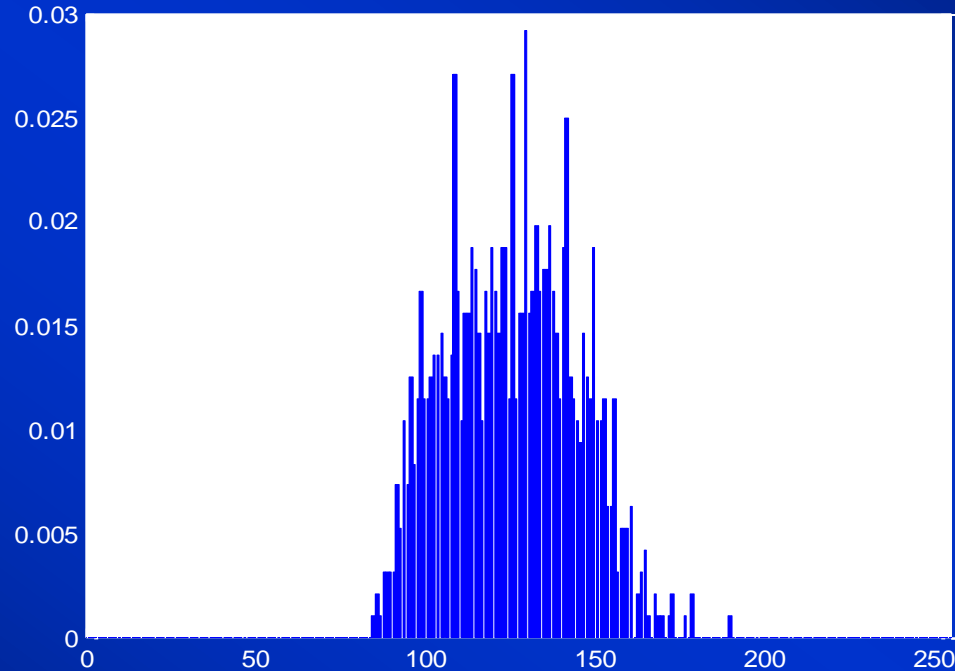
- Algorithm attempts to bring error to “zero”, defined by  $R_p^w$
- Problem:



- Solution : Local background is calculated by a mean shift process on histogram of local neighborhood

# Local Background - 2

- Problem : Local histogram not a “good” approximation of PDF

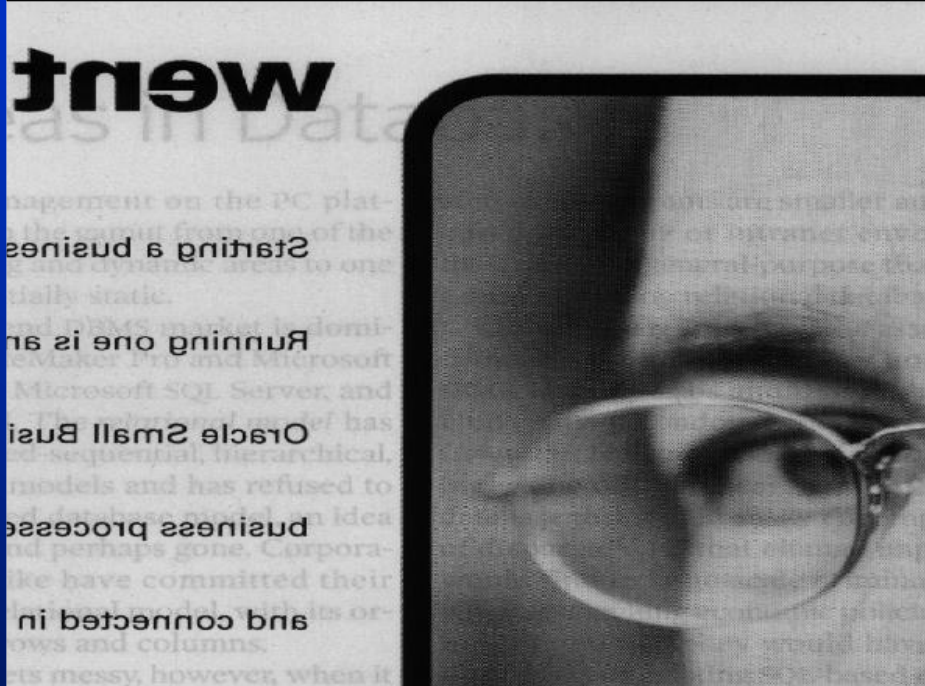


- Solution : Adaptive mean-shift – variable window size
  - Increase window size until it covers enough pixels
- When reverse-side activity is high, Global value is used



# Local Background - 3

Scanned Image



Background Image



- Global Background = 209



# Decorrelation Systems

Construction System

$$\begin{cases} X_1 = S_1 + H_1 S_2 \\ X_2 = S_2 \end{cases}$$

Recovery System

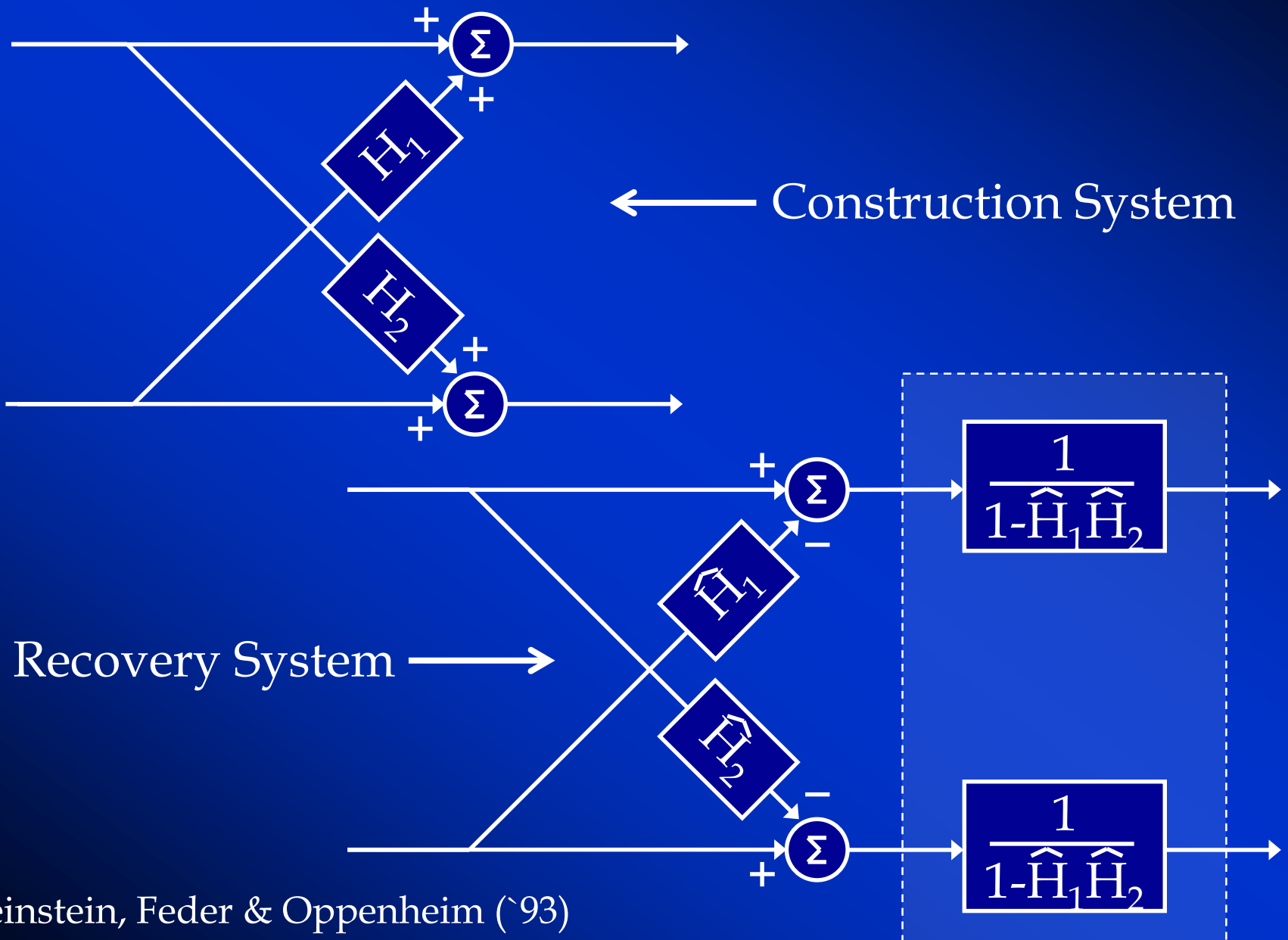
$$S_1 = X_2 - H_2 X_1$$

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$$\begin{cases} X_1 = S_1 + H_1 S_2 \\ X_2 = S_2 + H_2 S_1 \end{cases}$$

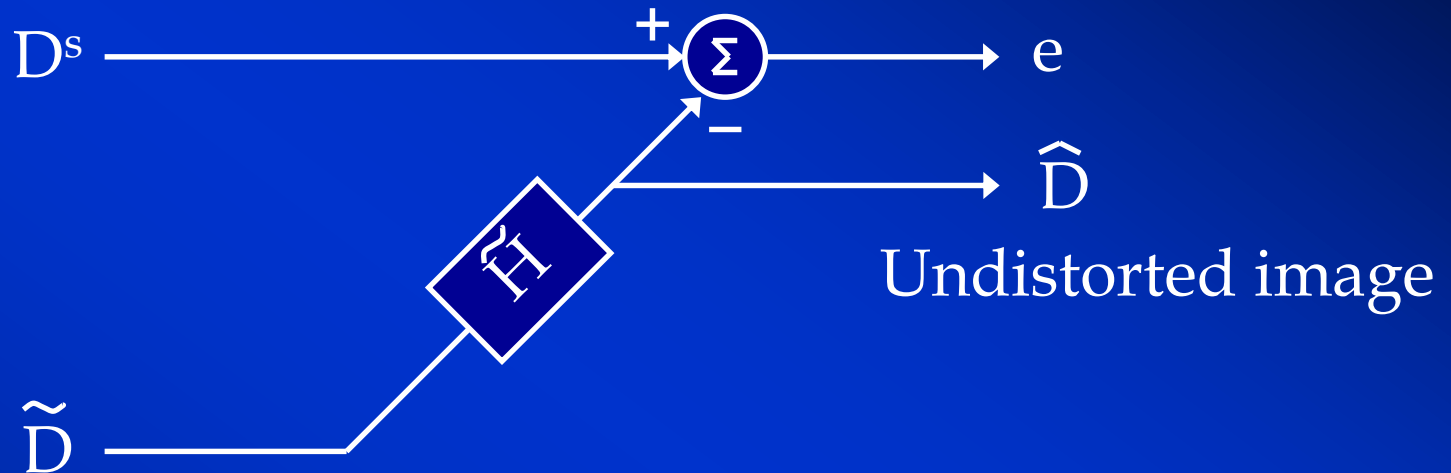
$$\begin{cases} S_1 = \frac{X_1 - H_1 X_2}{(1 - H_1 H_2)} \\ S_2 = \frac{X_2 - H_2 X_1}{(1 - H_1 H_2)} \end{cases}$$

# Decorrelation Systems



# Adaptive Post-Processing

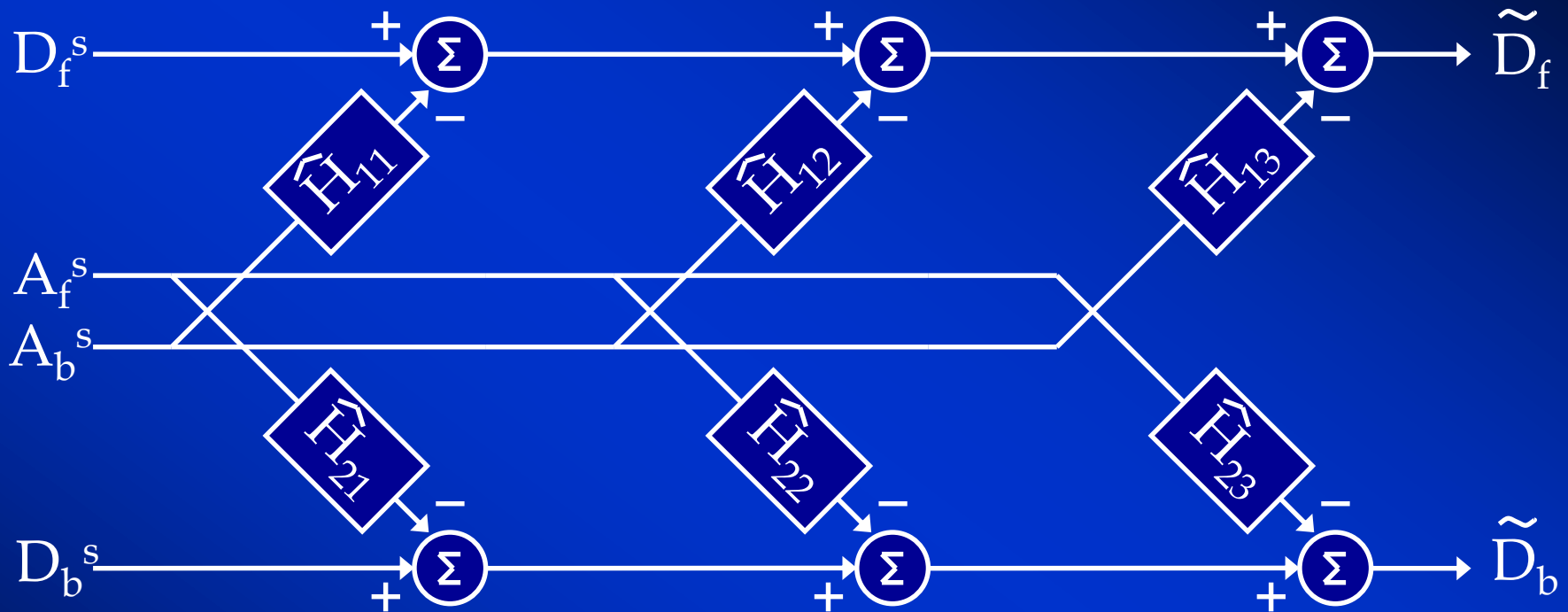
Scanned image



Decorrelated image

- Removes inherent distortion
- Removes some artifacts
- Degrades decorrelation somewhat

# Cascaded Filter Structure



- Filter support increases with each stage
  - Typical values - 5x5, 9x9 & 15x15 pixels

# Experimental Results

## e-business をサポ-

- A4 対応、最高印刷速度 20PPM で、リアル
- Adobe Systems 社純正 Postscript 3、PCL5e
- IBM PowerPC を採用した高速・高性能コン
- プリンター搭載 Web サーバー機能による、V
- 再生紙、ラベル紙、厚紙や不定型サイズ用紙
- 月間最大 100,000 ページ\*2 印刷の高耐久性

\*1 : 25.4mm 当りのドット数

\*2 : この値は月間の最大印刷可能です。毎月連続して最大量を印刷し続け

### 概要

このプリンターは、最高印刷速度 20PPM  
1200x1200DPI の高解像度の印刷が可能です。ま  
印刷でき耐久性にすぐれたレーザー・プリンター

	Before	After
Corr	0.17	0.015
MI	0.09	0.025



# Experimental Results

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	Before	Sharma	After
Corr	0.25	0.05	0.03
MI	0.1	0.02	0.01





# Decorrelation Algorithm Summary

- Improved algorithm includes:
  - Local background normalization
  - Adaptive post-processing stage
  - Cascaded filter structure
- Algorithm achieves improved results.
- Algorithm handles scans of complex documents containing text and images.

**Show-Through Removal**  
**by**  
**Blind Source Separation**  
**(BSS)**

# Show-Through as a BSS Problem



- Goal – estimate images **Y** and mixing parameters **H**
- Method: Minimization of a Cost Function

$$J = \left\| H(\mathbf{Y}) - \mathbf{X} \right\|_2^2$$

# Image Separation as a Regularization Problem

$$J = \|H(\mathbf{Y}) - \mathbf{X}\|_2^2 + \lambda_1 \text{Reg}(Y_1) + \lambda_2 \text{Reg}(Y_2)$$

- Assumption: Images  $Y_1$  and  $Y_2$  are independent

- Regularization Functions:

- Smoothness

- Markov Random Fields

- Total Variation

Simple  
Oversmoothing

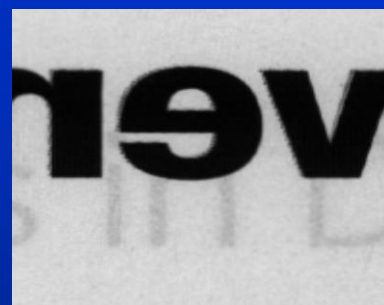
Edge Preserving  
Many Parameters  
Non Convex

Edge Preserving  
Convex

# Fidelity/Regularization Tradeoff

$$J = \|H(\mathbf{Y}) - \mathbf{X}\|_2^2 + \lambda_1 TV(Y_1) + \lambda_2 TV(Y_2)$$

- Tradeoff ratio  $\lambda$  determines strength of edges to be preserved.
- Strong *et al* ('97) suggest location dependent  $\lambda$  inversely proportional to gradient strength, in the context of image restoration.
  - $\lambda$  is set separately for vertical and horizontal edges.
- **Problem:** Show-Through interference contains edges itself.



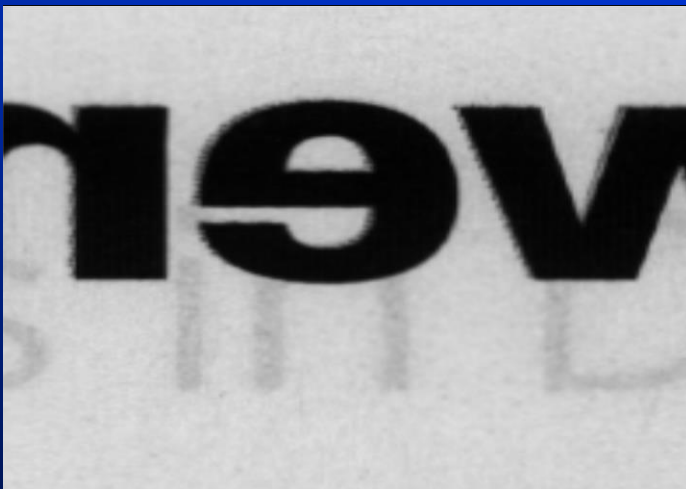
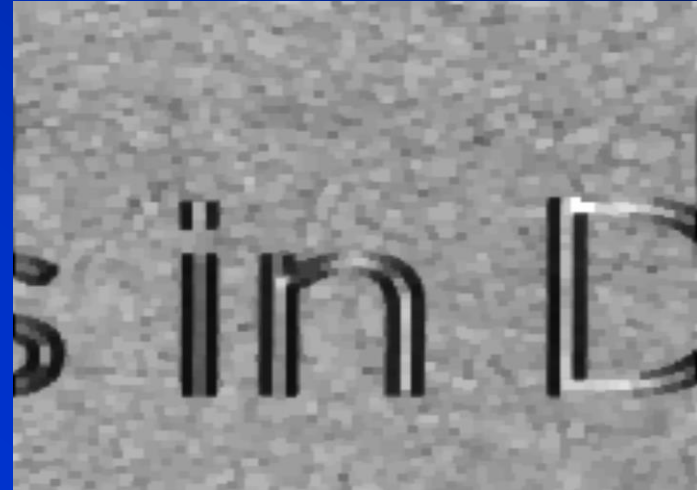
# Fidelity/Regularization Tradeoff

$$J = \|\mathbf{H}(\mathbf{Y}) - \mathbf{X}\|_2^2 + \lambda_1 TV(Y_1) + \lambda_2 TV(Y_2)$$

- **Solution:** Weighting is set using both images.
- Strong edge in one image and weak edge at the same location in the other image  $\Rightarrow$  Probable Show Through scenario
  - Set **high**  $\lambda$  at show through edge
    - proportional to true (reverse side) edge strength
  - Set **low**  $\lambda$  at true edge
    - inversely proportional to edge strength



# Example lambda maps



Scanned Images

Horizontal gradient  
 $\lambda$  maps

# Alternating Minimization

$$J = \|H(\mathbf{Y}) - \mathbf{X}\|_2^2 + \lambda_1 TV(Y_1) + \lambda_2 TV(Y_2)$$

- Simultaneous minimization is very difficult:
  - Non-linear in joint space  $\{H, \mathbf{Y}\}$
  - Non-convex in joint space  $\{H, \mathbf{Y}\}$
  - Large number of variables

- Reduction method:

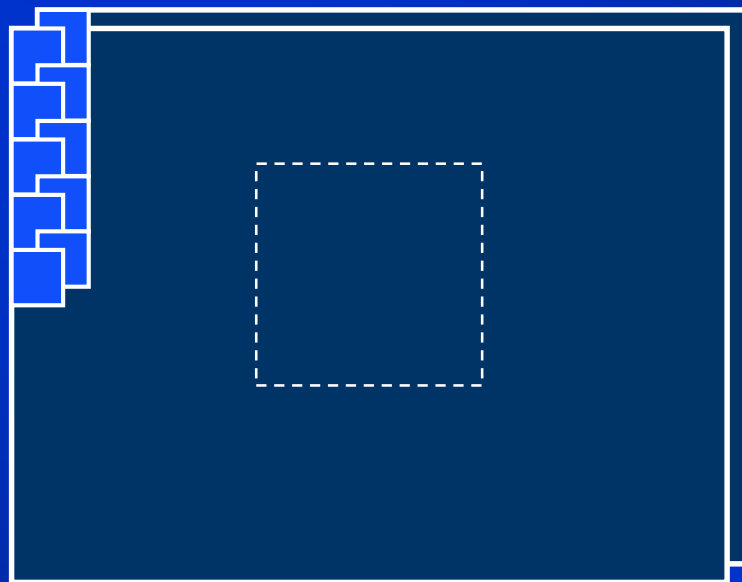
## Alternating Minimization in $\mathbf{Y}$ and $H$

- Linear optimization problems
- Convex cost functional

# Iterated Conditional Modes (ICM)

Besag (1986)

- Y optimization is done on a very large number of dependent variables



- $J$  is minimized one pixel location at a time.
- Each minimization is done only on partial sum of elements of  $J$ .
- Pixel values updated in place.
- Algorithm typically converges after 3-5 passes.
- To avoid directional preference we alternate pass direction.

# Mixing Parameter Estimation

$$J = \left\| \mathbf{M}(\mathbf{Y}) - \mathbf{Y} \mathbf{X} \left\|_2^2 \mathbf{X} \right\|_2^2 \right\|_2^2$$

- Assumption:  $H$  is the same throughout the image

$$H = \begin{pmatrix} 1 & h_{12} * f(\cdot) \\ h_{21} * f(\cdot) & 1 \end{pmatrix}$$

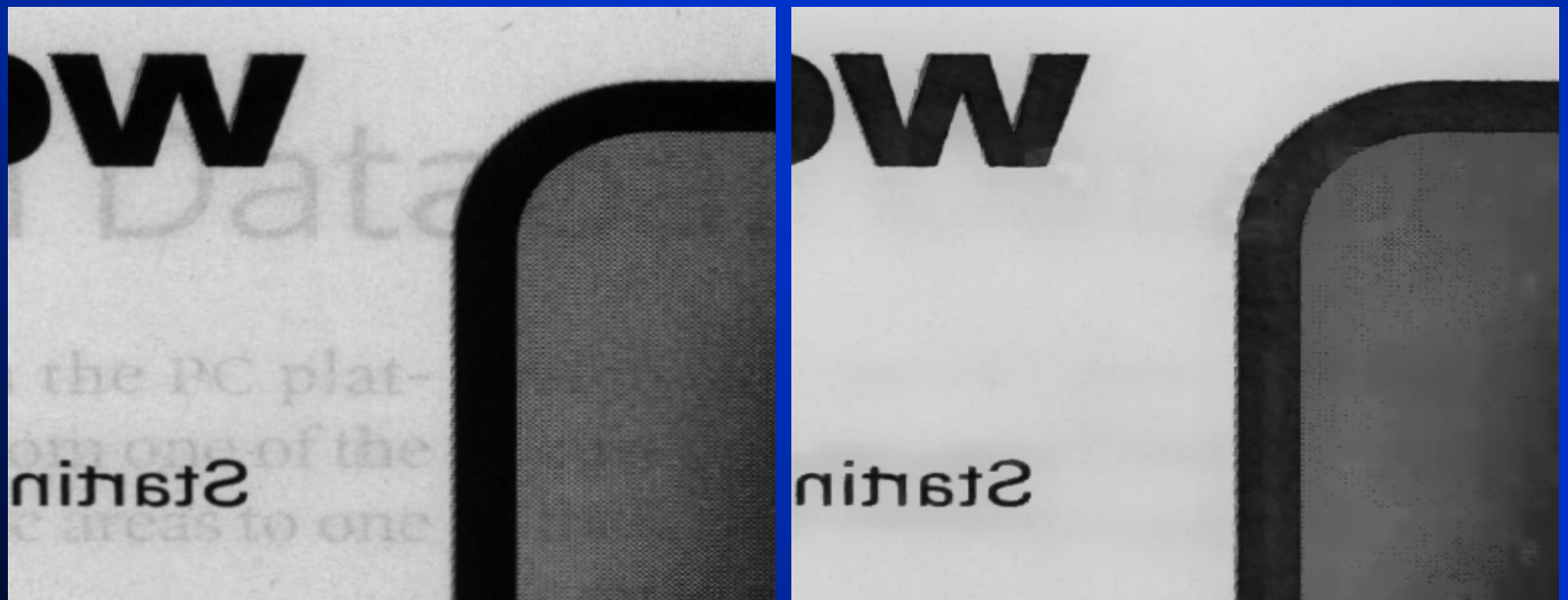
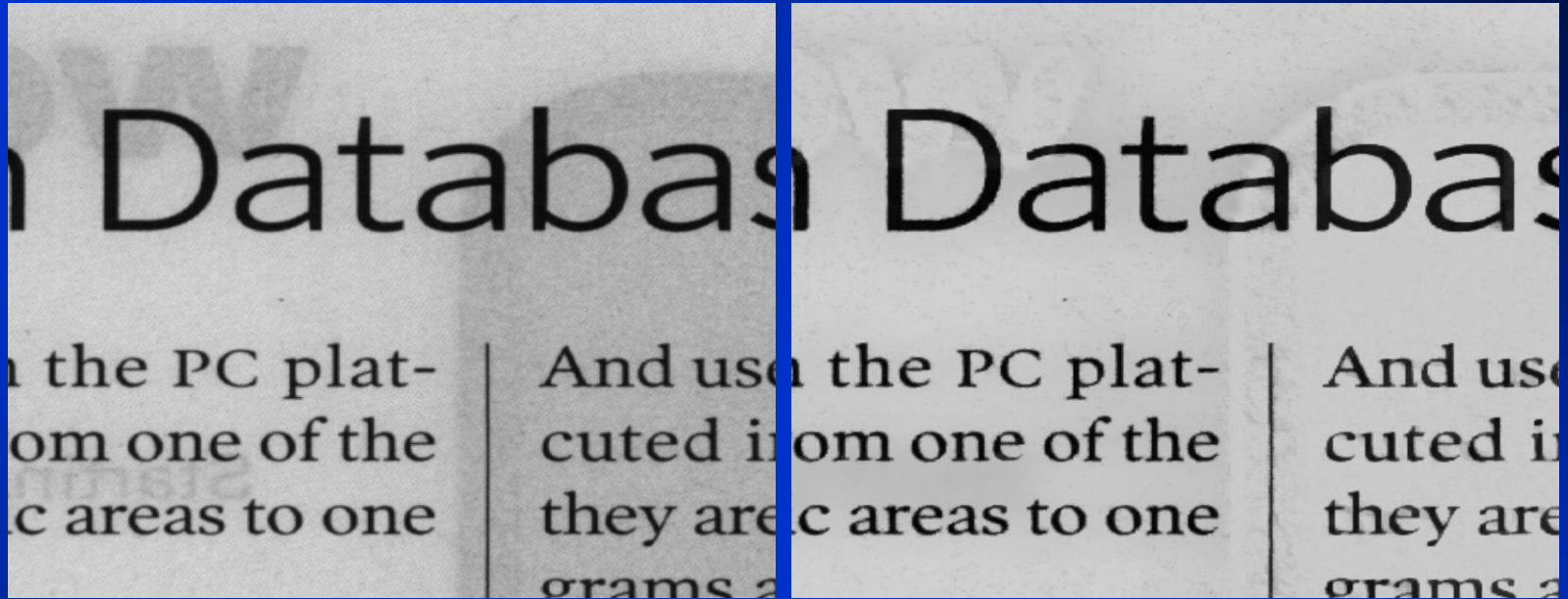
- Least Squares problem
- Many pixels do not contribute to the solution
- Activity Masks – only pixels with single sided activity

# Minimization Algorithm

- Estimate Background
- Initialization :  $Y=X, H = \begin{pmatrix} 1 & \varepsilon \\ \varepsilon & 1 \end{pmatrix}$
- Alternating Optimization:
  - **Y Optimization:**
    - Compute  $\lambda$  maps
    - ICM Iterations
      - Top-Bottom scan
      - Bottom-Top scan
  - **H Optimization:**
    - Compute activity masks
    - Least-Squares minimization
  - Normalize PSFs and images
- Repeat for larger filter support



# Experimental Results





# Experimental Results

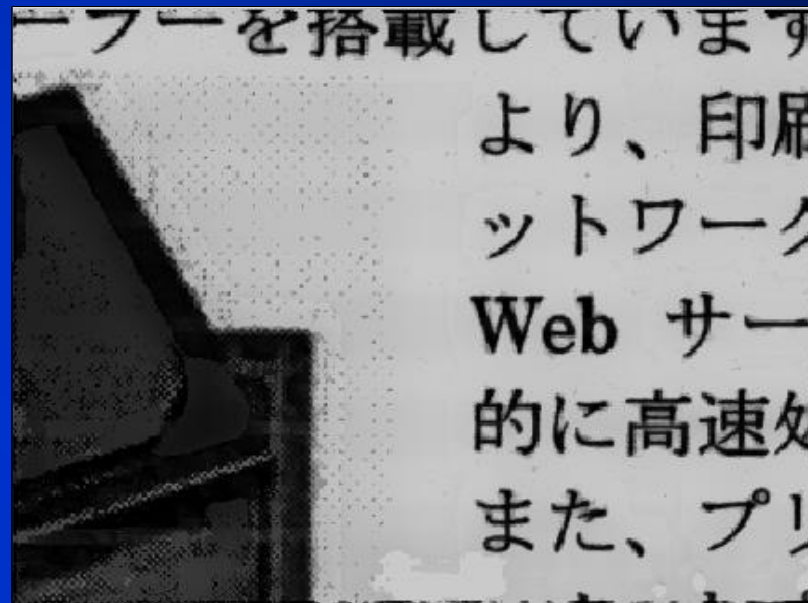
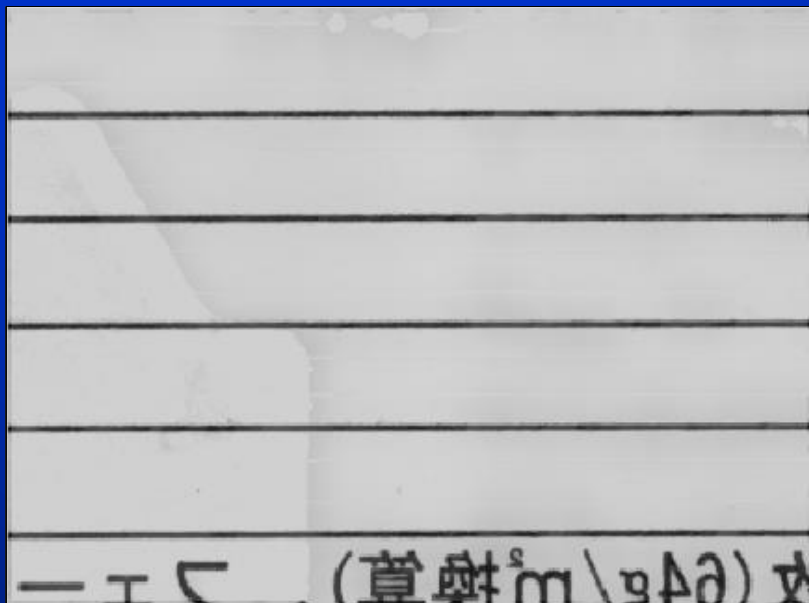
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# Experimental Results



# Conclusions and Future Work

# Conclusions

- Show-Through as a non-linear convolutive mixture of images.
- Two algorithms were proposed:
  - Decorrelation – good results at low computation cost
  - BSS – high computation, way of the future

# Future Work

- **Technical Improvements**
  - Better numerical approximations
  - Better optimization schemes
- **Theoretical Extensions**
  - Better image models
  - **Color** Images



**Thank You**

# Algorithm Complexity

## Decorrelation Algorithm:

- Per filtering stage
  - Per Pixel
    - Compute cleaned pixel value
    - Update PSF values

## BSS Algorithm:

- Per ICM iteration
  - Per Pixel location
    - Minimization of partial sum of J
      - Number of elements in partial sum depends on PSF support
      - Optimization by Line-Search
        - Gradient estimation (2 function calculations)
        - Line-Search iterations (typically 4-6 steps)